

Computer Assisted Reasoning

A Festschrift for Michael J. C. Gordon

Richard Boulton · Joe Hurd · Konrad Slind

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Today's increasingly computer-based society is dependent on the correctness and reliability of crucial infrastructure, such as programming languages, compilers, networks, and microprocessors. One important way to achieve the required level of assurance is to use formal specification and proof, and tool support for this approach has steadily grown to the point where the specification and verification of important system infrastructure is now feasible.

To survey the state of the art and discuss future possibilities and challenges, a two day research meeting entitled *Tools and Techniques for Verification of System Infrastructure*¹ was held in March 2008 at the Royal Society in London. The event was held in honour of Prof. Michael J. C. Gordon FRS on the occasion of his 60th birthday, and we are pleased to dedicate this special issue of the Journal of Automated Reasoning to him, which contains a selection of papers that followed from the meeting.

Career Overview Mike Gordon's career has been characterized by ground-breaking research on formal semantics for programming languages and machine-assisted formal verification. This focus has given us a creative and wide-ranging body of work. In 1970, Mike took the undergraduate degree in Mathematics at Cambridge University as a student of Gonville and Caius college. In 1973, he obtained a Ph.D. (supervisor: Rod Burstall) in the Edinburgh Department of Machine Intelligence for a dissertation entitled *Evaluation and Denotation of Pure LISP Programs*.² Mike returned to Cambridge the following year to obtain a Diploma in Linguistics, and then spent a year in Stanford before taking up a post-doctoral fellowship in Edinburgh to work on the LCF project led by Robin Milner. Following a short period as an SRC Advanced Research Fellow at Edinburgh, Mike took up a lectureship in the Cambridge University Computer Laboratory in 1981. He has been there ever since, becoming a Reader in 1988, and Professor of Computer Assisted Reasoning in 1996. Mike was elected a Fellow of the Royal Society in 1994.

Icera Inc., 2520 The Quadrant, Aztec West, Bristol, BS32 4AQ, U.K. · Galois, Inc., 421 S.W. 6th Ave., Ste. 300, Portland OR 97204, U.S.A. · Rockwell Collins Advanced Technology Center, 400 Collins Road, N.E. Cedar Rapids, IA 52498, U.S.A.

¹ <http://www.ttvsi.org/>

² Examiners: David Park and Robin Milner.

Programming Language Semantics Mike's Ph.D. explored the semantics of Lisp using domain theory, which had recently been created by Dana Scott. Lisp's dynamic binding was a particular focus in this work [14]. Some years later Mike also published an accessible undergraduate semantics textbook which focused on denotational methods [15].

Edinburgh LCF In the mid 1970s Mike and Chris Wadsworth replaced Lockwood Morris and Malcolm Newey as research assistants to Robin Milner working on Edinburgh LCF, a system designed by Milner as a successor to his earlier Stanford LCF. The project resulted in the ML language [23], a hugely influential force in computer science, plus the LCF theorem prover. LCF was both the name of the interactive proof system and the name of the logic (Logic for Computable Functions). The original system is discussed in [24]; an enhanced version due to Larry Paulson is documented in [39]. These original systems have not been maintained, but a version of the LCF logic continues to be distributed as an instance of the Isabelle generic proof system [40].

Hardware Verification Mike's research focus then shifted to hardware verification. He originally expressed hardware in *LCF.LSM*, a modification of the LCF system which incorporated ideas from CCS [33]. Using this system, he specified and verified a simple general-purpose computer, which subsequently became known as Gordon's computer [18]. Mike abandoned LCF.LSM in favour of higher order logic (HOL) following discussions with Ben Moszkowski; the benefits of higher-order functions for hardware are discussed in [19]. The modelling style advocated in that paper, namely to formalize devices as predicates on streams has been highly successful.

Hardware verification via interactive theorem proving attracted a great deal of interest at this time, and much of the leading work was being performed by Mike and his group at Cambridge. The techniques developed by them were applied to more sophisticated examples; for example, by Graham Birtwistle and Brian Graham at Calgary [28]. There were applications to the Viper military microprocessor [6, 7] as a joint project between Mike's colleague (and wife) Avra Cohn and the Royal Signals and Radar Establishment (RSRE). This generated some controversy about the scope and limits of hardware verification [31] following the publication of an influential paper in this journal [8].

More recently, as a joint project with Birtwistle at Leeds, a model of an ARM instruction set architecture was shown to be correctly implemented by a model of the ARM6 microarchitecture [10, 11]. This has led to new methods for reasoning about low level software running on accurate hardware models [34]. In a related thrust, deduction-based algorithms are used to synthesize low-level implementations directly from functions defined in logic [34, 42].

Higher Order Logic Much of the work on hardware verification conducted by Mike and his colleagues was performed using the HOL system. Besides being users of HOL, Mike and his students were also developing HOL, in particular the *HOL88* system [27]. Initially applied solely in the domain of hardware verification, higher order logic has since been applied to formalization and proof in a wide variety of settings, including pure and applied mathematics, hardware, and software. The HOL88 system spawned a number of mature descendants, including ProofPower [2], HOL-4 [41], Isabelle/HOL [36], and HOL Light [29].

A pervasive attitude—advocated early on by Mike—in the implementation of all these systems is the so-called *LCF approach*: the use of derived rules of definition and

inference, which reduce all reasoning to primitive inference steps provided by a small kernel [17]. The LCF approach is tremendously flexible, and methods for efficient LCF-style proof have emerged [5,30].

In order to gather together the users of HOL for discussions, Mike initiated the *HOL Users Group* (HUG) series of meetings. This evolved into *TPHOLs* (Theorem Proving in Higher Order Logics), which provides a venue for research on any aspect of theorem proving with a flavour of higher order logic. TPHOLs has enjoyed robust health: this year (2009) finds the twenty-second instance being held in Munich.³

Formalized Semantics and Language Embeddings Mike and his students have a long history of formalizing language syntax and semantics. For example, Mike's influential paper [16] showed how a logic for a programming language could be derived from its formal semantics. The semantics of hardware description languages has been an ongoing activity. In early work, ELLA, VHDL, and SILAGE were discussed in [3]; the simulation-cycle semantics of Verilog appears in [20]; and a HOL formalization of the industry-standard PSL language appears in [22]. The semantics of many other computer languages have been formalized by Mike's students, among them CCS [35], π -calculus [32], C [37], C++ [38], and Java [43].

External Interfaces Mike has been a leader in the area of integration of theorem provers, efficient formula representations, and logics. In a joint project with Alan Bundy at Edinburgh, the HOL-Clam system [4] integrated the proof-planning capabilities of the Clam system with HOL. Mike was a member of the PROSPER project [9], led by Tom Melham, which provided exchange mechanisms for logical terms, formulas, and theories and investigated the coordination of a wide variety of reasoning and symbolic analysis tools. Mike oversaw the integration of BDDs into HOL, leading to a number of papers [21,1] showing how model-checking algorithms could be hosted on an LCF-style core inside HOL. In recent work, Mike has been collaborating with the authors of ACL2 in order to derive and exploit a verified translation between ACL2 and HOL [26,25].

Teaching Mike has long been recognized as a leader in teaching formal methods. His undergraduate course notes *Specification and Verification* [12,13] have been refined over years, and provide a time-tested and detailed resource for teaching program logic and hardware verification. These notes are characteristically clear and extremely detailed; we can personally testify that they have been re-used in many institutions worldwide.

Students The following is an alphabetical list of Mike's graduated Ph.D. students:

Hasan Amjad	Jim Grundy	Michael Norrish
Richard Boulton	John Harrison	James Reynolds
Albert Camilleri	Joe Hurd	Mark Staples
Rachel Cardell-Oliver	Juliano Iyoda	Daryl Stewart
Victor Carreño	Jeff Joyce	Donald Syme
Francisco Corella	Tom Melham	John Van Tassel
Inder Dhingra	Magnus Myreen	Stuart Wray
Jon Fairbairn	Monica Nesi	

³ From 2010 the conference will be known as *Interactive Theorem Proving* (ITP).

Finally For us, and many others, Mike has been an ongoing source of research ideas and encouragement. His advice is unfailingly good. As a Ph.D. advisor and mentor, he has provided guidance of all kinds to his students and many others. Certainly, his Hardware Verification Group (HVG)⁴ has over the years been a welcoming home, both to his students and to the many visitors who have come to Cambridge in order to share in the joys of doing research with Mike. We hope it goes on for many years to come!

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